

## Notes 3.2 – Graphing Polynomials

Warmup – Simplify each expression

1.  $(6x + 3) + (4x + 5)$

$10x + 8$

2.  $(x + 17) + (9x - 13)$

$10x + 4$

3.  $(7x - 8) + (-2x + 9)$

$5x + 1$

4.  $(4x + 9) - (x + 2)$

$3x + 7$

5.  $(-3x - 1) - (2x + 5)$

$-5x - 6$

6.  $(8x + 3) - (-10x - 9)$

$18x + 12$

7.  $(3x - 7) + (-3x - 7)$

$-14$

2.  $(-5x + 8) - (-5x + 7)$

$1$

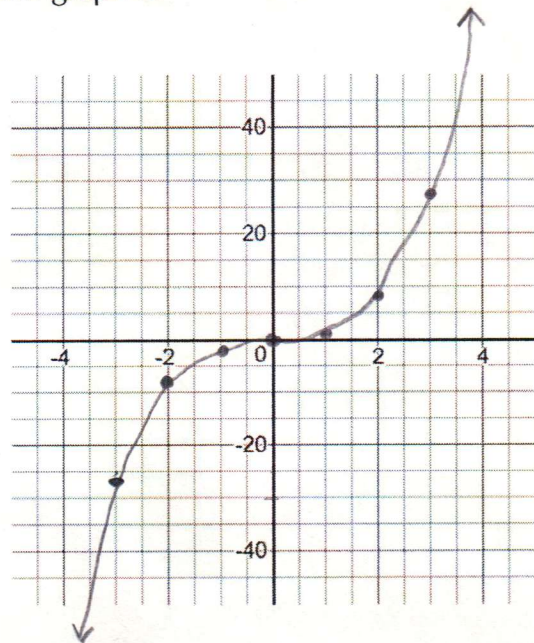
3.  $(8x + 9) - (7x + 9)$

$x$

Investigation

- a. Create a table for the function
- $f(x) = x^3$
- , then graph it.

$x$	$y$
-3	-27
-2	-8
-1	-1
0	0
1	1
2	8
3	27



- b. Give the features of the function
- $f(x) = x^3$
- .

domain:  $\mathbb{R}$ range:  $\mathbb{R}$ x-int:  $(0,0)$ y-int:  $(0,0)$ 

cubic

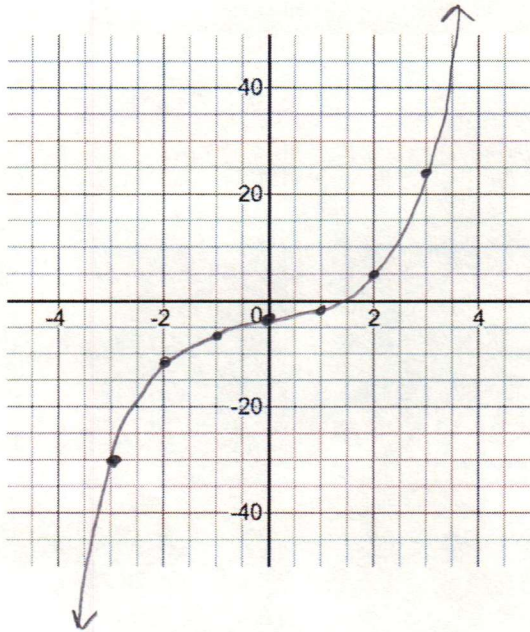
inc:  $\mathbb{R}$ 

cubic

- c. Using the parent function  $(x) = x^3$ , and your knowledge of transformation from the last unit and last year, graph each function below.

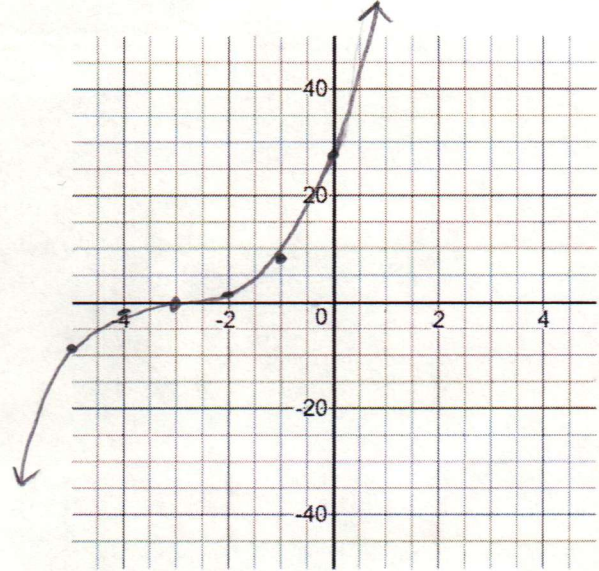
$$f(x) = x^3 - 3$$

Transformation: down 3



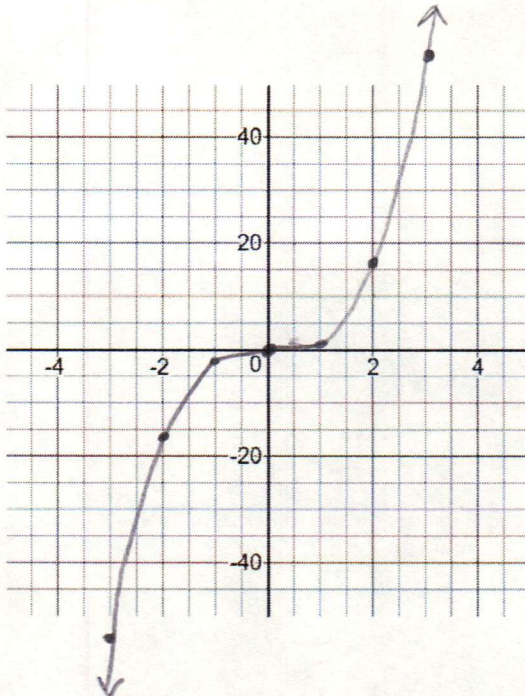
$$f(x) = (x + 3)^3$$

Transformation: left 3



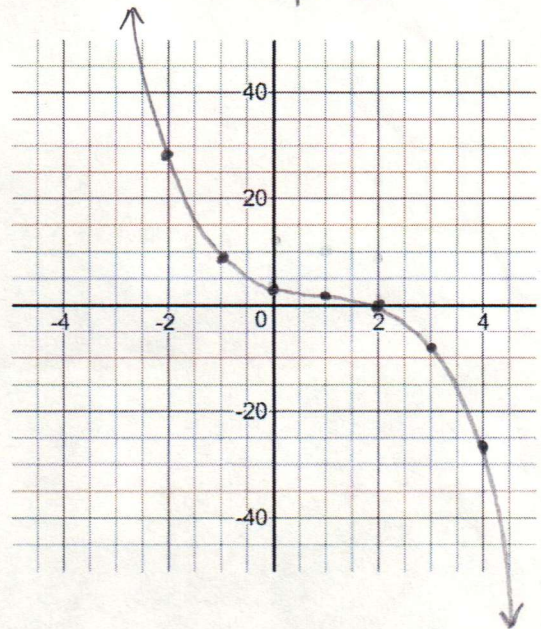
$$f(x) = 2x^3$$

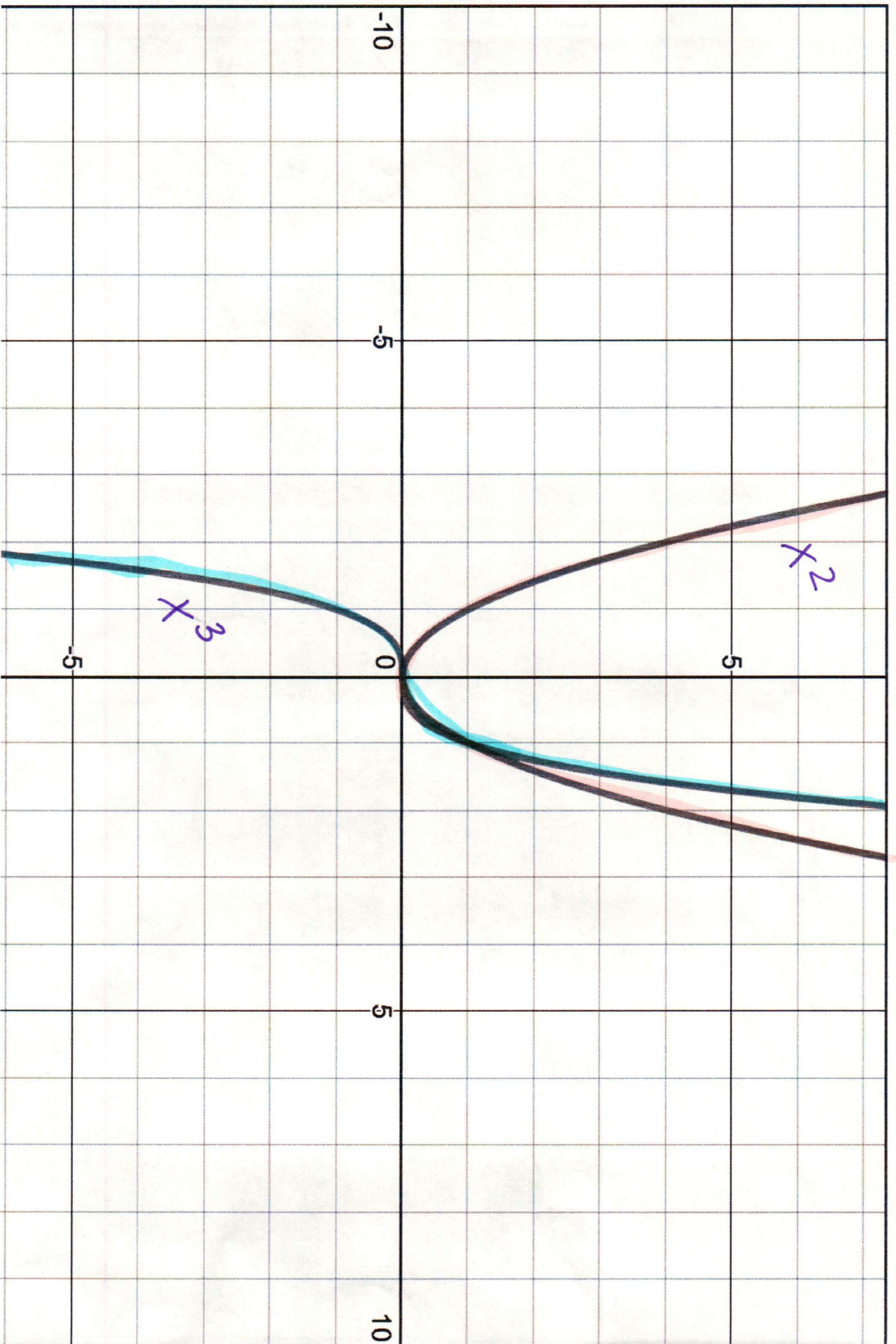
Transformation: stretch  $\times 2$



$$f(x) = -(x - 1)^3 + 2$$

Transformations: reflect  
right 1  
up 2





d. List the similarities you see between  $f(x) = x^3$  and  $g(x) = x^2$ ?

both are curved

right half of  $x^3$  looks similar to right half of  $x^2$

domains are the same

same anchor point  $(0,0)$

{ Same x/y intercepts  
both have  $(1,1)$   
both increasing after  $(0,0)$

e. Below are three differences between  $f(x) = x^3$  and  $g(x) = x^2$ , explain why each is true.

The range of  $f(x) = x^3$  is  $(-\infty, \infty)$ , but the range of  $g(x) = x^2$  is  $[0, \infty)$  because

both sides of  $x^2$  go up, it has a minimum

For  $x > 1$ ,  $f(x) > g(x)$  because

$x^3$  gives greater values than  $x^2$  after  $x=1$

$$2^2 = 4 \text{ and } 2^3 = 8$$

For  $0 < x < 1$ ,  $g(x) > f(x)$  because

a fraction squared has a higher value

than a fraction cubed

$$\left(\frac{1}{2}\right)^2 = \frac{1}{4} \quad \left(\frac{1}{2}\right)^3 = \frac{1}{8}$$